

A, B, so C	A, since B and C	A, so B, since C
A and B	A but B	A but not B
A even though not B	A or B	either A or B
it is not the case that not A	that not A is not true	it is not false that not A
not both A and B	not both A and not B	both not A and not B
neither A nor B	not either A or B	either not A or not B

A , C ∴ B

B , C ∴ A

A , B ∴ C

A & ~B

A & B

A & B

A ∨ B

A ∨ B

A & ~B

~(~(~A))

~(~A)

~(~A)

~~~A

~~A

~~A

~A & ~B

~(A & ~B)

~(A & B)

~A ∨ ~B

~(A ∨ B)

~A & ~B

~(A ∨ B)

|                           |                        |                        |
|---------------------------|------------------------|------------------------|
| not either not A or not B | A, B, and C            | A, B, or C             |
| one of A, B, and C        | not all of A, B, and C | not any of A, B, and C |
| without B, not A          | if A then B            | B, if A                |
| if not A, then not B      | not B, if not A        | not A unless B         |
| not A unless not B        | A unless B             | A unless not B         |
| A only if B               | not A only if B        | A only if not B        |

$A \vee B \vee C$

$A \wedge B \wedge C$

$\sim(\sim A \vee \sim B)$

$\sim A \wedge \sim B \wedge \sim C$

$\sim(A \wedge B \wedge C)$

$A \vee B \vee C$

$A \supset B$

$A \supset B$

$A \supset B$

$\sim B \supset \sim A$

$A \supset B$   
 $\sim B \supset \sim A$

$\sim A \supset \sim B$

$\sim A \supset \sim B$

$B \supset A$   
 $\sim A \supset \sim B$

$\sim B \supset A$   
 $\sim A \supset B$

$A \supset \sim B$   
 $B \supset \sim A$

$A \supset \sim B$   
 $B \supset \sim A$

$\sim A \supset B$   
 $\sim B \supset A$

$A \supset B$   
 $\sim B \supset \sim A$

|                          |                           |                           |
|--------------------------|---------------------------|---------------------------|
| unless B, not A          | unless B, A               | only if B, A              |
| not A without B          | A occurred without B      | A if and only if B        |
| A, but only if B         | if and only if B, A       | A exactly when B          |
| if A and B, then C       | if A, and if B, then C    | if A, then if B, then C   |
| if A, then B and C       | if A, then either B or C  | if either A or B, then C  |
| either A or both B and C | both either A or B, and C | either both A and B, or C |

|                                  |                                                                 |                         |
|----------------------------------|-----------------------------------------------------------------|-------------------------|
| $A \supset B$                    | $\sim B \supset A$                                              | $A \supset B$           |
| $\sim B \supset \sim A$          |                                                                 | $\sim B \supset \sim A$ |
|                                  |                                                                 |                         |
| $A \equiv B$                     | $A \& \sim B$                                                   | $A \supset B$           |
| $(A \supset B) \& (B \supset A)$ | when $A$ is on the left side,<br>and is affirmative and factual | $\sim B \supset \sim A$ |
|                                  |                                                                 |                         |
| $A \equiv B$                     | $A \equiv B$                                                    | $A \equiv B$            |
|                                  |                                                                 |                         |
| $A \supset (B \supset C)$        | $(A \& B) \supset C$<br>$A \supset (B \supset C)$               | $(A \& B) \supset C$    |
|                                  |                                                                 |                         |
| $(A \vee B) \supset C$           | $A \supset (B \vee C)$                                          | $A \supset (B \& C)$    |
|                                  |                                                                 |                         |
| $(A \& B) \vee C$                | $(A \vee B) \& C$                                               | $A \vee (B \& C)$       |