

Worksheet Exercise 4.3.

Name _____

Calculating Truth-values

Class _____ Date _____

Part A. Translate each of the following sentences into a regular English sentence, using the listed meanings for the symbols; and then, state their truth-value, **T** or **F**.

T = triangle, F = figure, C = circle, S = square,
 U = four-sided, G = green, B = blue, c = Chicago

truth-value

- | | | |
|--|-------|-------|
| 1. $(\forall x)(Fx \supset Tx)$ | _____ | _____ |
| 2. $(\forall x)(Cx \supset \sim Sx)$ | _____ | _____ |
| 3. $(\exists x)(Sx \ \& \ Ux)$ | _____ | _____ |
| 4. $(\forall x)(Sx \ \& \ Gx)$ | _____ | _____ |
| 5. $(\exists x)(\sim Sx \ \& \ \sim Cx)$ | _____ | _____ |
| 6. $(\forall x)(Bx \ \vee \ Gx)$ | _____ | _____ |
| 7. $(\forall x)(\sim Bx \ \vee \ \sim Gx)$ | _____ | _____ |
| 8. Tc | _____ | _____ |

Part B. In the spaces provided, calculate the truth-values of the following sentences, using the calculated truth-values from Part A. Use the Tree Method.

9. $Tc \supset (\exists x)(Sx \ \& \ Ux)$

10. $(\forall x)(Fx \supset Tx) \vee (\forall x)(Bx \ \vee \ Gx)$

11. $(\exists x)(Sx \ \& \ Ux) \equiv (\exists x)(\sim Sx \ \& \ \sim Cx)$

12. $\sim [(\forall x)(Bx \ \vee \ Gx) \ \& \ Tc]$

13. $\sim Tc \ \vee \ \sim (\forall x)(Cx \ \supset \ \sim Sx)$

14. $\sim (\forall x)(Fx \ \supset \ Tx) \ \supset \ \sim (\exists x)(Sx \ \& \ Ux)$

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Part C. In the spaces provided, calculate the truth-values of the following sentences. Use the Tree Method and the symbol meanings from Part A. You must first determine the values of the simple component sentences.

15. $(\forall x)(Fx \supset Sx) \equiv [(\forall x)(Tx \supset Ux) \vee \sim(Bc \ \& \ Tc)]$

16. $(\exists x)(Fx \ \& \ Cx) \ \& \ (\exists x)(Fx \ \& \ \sim Cx) \ \& \ \sim(\exists x)[Fx \ \& \ (Cx \ \& \ \sim Cx)]$

17. $[(\forall x)(Tx \supset Bx) \vee (\forall x)(Tx \supset \sim Bx)] \ \& \ (\forall x)[Tx \supset (Bx \vee \sim Bx)]$

18. $(\forall x)[(Sx \ \& \ Bx) \supset (Fx \ \& \ Ux \ \& \ \sim Gx)] \supset [(\exists x)(Sx \ \& \ Tx) \vee (\exists x)(Bx \ \& \ Gx)]$

19. $[(\forall x)(Cx \supset Bx) \ \& \ (\forall x)(Bx \supset Cx)] \equiv (\forall x)(Cx \equiv Bx)$

20. $\{(\exists x)[Fx \ \& \ (Tx \ \& \ \sim Ux \ \& \ \sim Cx)] \vee (\exists x)[Fx \ \& \ (\sim Tx \ \& \ Ux \ \& \ \sim Cx)]\} \supset \sim(\forall x)Gx$